

Egyptian Fractions

The Egyptians only used fractions with a numerator of 1.*

Take the fraction $80/100$ and keep subtracting the largest possible Egyptian fraction till you get to zero. Three Egyptian fractions are enough:

$$80/100 = 1/2 + 1/4 + 1/20$$

Do the same for $85/100$, $90/100$, $95/100$, and if you are particularly fond of Egyptians, $99/100$.



Egyptian Fractions were found on the Rhind Mathematical Papyrus.

This papyrus is a scroll that got its name from a sickly young man called Henry Rhind who bought the papyrus in Luxor, Egypt in 1858 shortly before his death at age 30.

The papyrus was written by a scribe called Ahmes sometime between 1600 and 1650 BC. He probably copied it from a still older source.

The papyrus is about 33 cm high and 5.6 meters long. Gay Robins & Charles Shute translate its initial lines as follows:

Correct method of reckoning, for grasping the meaning of things and knowing everything that is, obscurities... and all secrets.

Extensions:

Show that any fraction $2/N$ (where N is odd) can be expressed as the sum of two Egyptian fractions, one of which is the largest Egyptian fraction less than $2/N$.

Fibonacci proved that if you keep subtracting the largest possible Egyptian fraction you will always get to zero in a finite number of steps. Is this true if you limit yourself to Egyptian Fractions with an odd denominator? **Warning: This is an unsolved problem in mathematics.**

*This is not quite true; the Egyptians also used $2/3$, but we will ignore this little anomaly.

The Math in This Problem:

Egyptian Fractions are unique because they only possess numerators equalling 1. In this brainteaser, students will manipulate fractions in order to create a summation of Egyptian Fractions, starting with the largest possible term and ending with the smallest possible term.